

Chapter 8**Multiple Choice**

Identify the choice that best completes the statement or answers the question.

___ 1. Write the expression $\sqrt{-36} \cdot \sqrt{-25}$ in terms of i and then simplify.

- a. -30
- b. -35
- c. 35
- d. -24
- e. 30

___ 2. Combine the complex numbers.

$$(5 - 8i) - (2 - 4i)$$

- a. $4 - 5i$
- b. $4 - 4i$
- c. $3 - 5i$
- d. $3 - 4i$
- e. $4 + 5i$

___ 3. Find the product.

$$(7 - 5i)^2$$

- a. $-26 - 72i$
- b. $26 - 70i$
- c. $26 - 72i$
- d. $24 - 72i$
- e. $24 - 70i$

___ 4. Find the product.

$$(2 + 5i)(2 - 5i)$$

- a. $29 - 20i$
- b. 29
- c. 25
- d. 27
- e. $27 - 20i$

5. Write the complex number in standard form.

$$8 \left(\cos \frac{5\pi}{6} + i \sin \frac{5\pi}{6} \right)$$

- a. $-4 + 4i\sqrt{3}$
- b. $-4\sqrt{3} + 4i$
- c. $4 + 4i\sqrt{3}$
- d. $4\sqrt{3} + 4i$
- e. $-4 - 4i\sqrt{3}$

6. Use a calculator to help write the complex number in standard form. Round the numbers in your answer to the nearest hundredth.

$$10 \operatorname{cis} 5.9$$

- a. $9.27 - 3.78i$
- b. $9.19 - 3.82i$
- c. $9.31 - 3.78i$
- d. $9.27 - 3.74i$
- e. $9.31 - 3.74i$

7. Multiply. Leave the answer in trigonometric form.

$$4(\cos 20^\circ + i \sin 20^\circ) \cdot 7(\cos 35^\circ + i \sin 35^\circ)$$

- a. $28(\cos 55^\circ + i \sin 55^\circ)$
- b. $24(\cos 50^\circ + i \sin 50^\circ)$
- c. $28(\cos 45^\circ + i \sin 45^\circ)$
- d. $24(\cos 55^\circ + i \sin 55^\circ)$
- e. $28(\cos 50^\circ + i \sin 50^\circ)$

8. Write z_1 and z_2 in trigonometric form and find their product.

$$z_1 = -1 + i\sqrt{3}, \quad z_2 = 1 - i\sqrt{3}$$

- a. $2(\cos 330^\circ + i \sin 330^\circ)$
- b. $2(\cos 30^\circ + i \sin 30^\circ)$
- c. $4(\cos 240^\circ + i \sin 240^\circ)$
- d. $4(\cos 150^\circ + i \sin 150^\circ)$
- e. $4(\cos 60^\circ + i \sin 60^\circ)$

- ___ 9. Use DeMoivre's Theorem to find the following. Write your answer in standard form.

$$\left(\sqrt{2} \operatorname{cis} \frac{9\pi}{20}\right)^5$$

- a. $-4 + 4i$
- b. $-16\sqrt{3} - 16i$
- c. $-4 + 4i\sqrt{3}$
- d. $-16 - 16i\sqrt{3}$
- e. $4 + 4i$

- ___ 10. Use DeMoivre's Theorem to find the following. Write your answer in standard form.

$$(-\sqrt{3} + i)^6$$

- a. $8i$
- b. $-16 - 16i\sqrt{3}$
- c. -64
- d. $-8 - 8i\sqrt{3}$
- e. 64

- ___ 11. Find the quotient $\frac{z_1}{z_2}$ in standard form.

$$z_1 = 8 + 8i, z_2 = 4 + 4i$$

- a. 2
- b. -2
- c. -7
- d. $-2i$
- e. 7

- ___ 12. Write z_1 and z_2 in trigonometric form and then find their quotient.

$$z_1 = 3\sqrt{3} - 3i, z_2 = 6i$$

- a. $\cos 330^\circ + i \sin 330^\circ$
- b. $\cos 120^\circ + i \sin 120^\circ$
- c. $2(\cos 60^\circ + i \sin 60^\circ)$
- d. $2(\cos 180^\circ + i \sin 180^\circ)$
- e. $\cos 240^\circ + i \sin 240^\circ$

13. Convert complex numbers to trigonometric form and then simplify the expression. Write the answer in standard form.

$$\frac{(1-i)^4 (i)^2}{-2+2i}$$

- a. $-16 + 16i$
- b. $-1 - i$
- c. $-16 - 16i$
- d. $4 - 4i$
- e. $-4 + 4i$

14. DeMoivre's Theorem can be used to find reciprocals of complex numbers. Recall from algebra that the reciprocal of x is $\frac{1}{x}$, which can be expressed as x^{-1} .

Use this fact, along with DeMoivre's Theorem, to find the reciprocal of the number below.

$$1 - i$$

- a. $\frac{1}{4} + \frac{\sqrt{3}}{4}i$
- b. $-\frac{1}{2} - \frac{1}{2}i$
- c. $\frac{1}{2} + \frac{1}{2}i$
- d. $-\frac{1}{4} - \frac{\sqrt{3}}{4}i$
- e. $-\frac{\sqrt{3}}{4} - \frac{1}{4}i$

15. Find two square roots for the complex number. Write your answer in standard form.

$$-2 + 2i\sqrt{3}$$

- a. $\sqrt{3} + i, -\sqrt{3} - i$
- b. $1 + i\sqrt{3}, -1 - i\sqrt{3}$
- c. $\sqrt{2} + i\sqrt{2}, -1\sqrt{2} - i\sqrt{2}$
- d. $-1 + i\sqrt{3}, 1 - i\sqrt{3}$
- e. $-\sqrt{3} + i, \sqrt{3} - i$

16. Find two square roots for the complex number. Write your answer in standard form.

$$-64$$

- a. $8i, -8$
- b. $64i, -64i$
- c. $8, -8$
- d. $8, -8i$
- e. $8i, -8i$

17. Find three cube roots for the complex number. Leave your answers in trigonometric form.

$$27(\cos 297^\circ + i \sin 297^\circ)$$

- a. $3 \operatorname{cis} 97^\circ, 3 \operatorname{cis} 217^\circ, 3 \operatorname{cis} 337^\circ$
- b. $3 \operatorname{cis} 98^\circ, 3 \operatorname{cis} 218^\circ, 3 \operatorname{cis} 338^\circ$
- c. $3 \operatorname{cis} 99^\circ, 3 \operatorname{cis} 219^\circ, 3 \operatorname{cis} 339^\circ$
- d. $4 \operatorname{cis} 97^\circ, 4 \operatorname{cis} 217^\circ, 4 \operatorname{cis} 337^\circ$
- e. $4 \operatorname{cis} 99^\circ, 4 \operatorname{cis} 219^\circ, 4 \operatorname{cis} 339^\circ$

18. Find 4 fourth roots of $z = 1,296 \left(\cos \frac{2\pi}{3} + i \sin \frac{2\pi}{3} \right)$. Write each root in standard form.

- a. $1 + i\sqrt{3}, -\sqrt{3} + i, -1 - i\sqrt{3}, \sqrt{3} - i$
- b. $3 + 3i\sqrt{3}, -3\sqrt{3} + 3i, -3 - 3i\sqrt{3}, 3\sqrt{3} - 3i$
- c. $\sqrt{3} + i, -1 + i\sqrt{3}, -\sqrt{3} - i, 1 - i\sqrt{3}$
- d. $3\sqrt{3} + 3i, -3 + 3i\sqrt{3}, -3\sqrt{3} - 3i, 3 - 3i\sqrt{3}$
- e. $3\sqrt{2} + 3i\sqrt{2}, -3\sqrt{2} + 3i\sqrt{2}, -3\sqrt{2} - 3i\sqrt{2}, 3\sqrt{2} - 3i\sqrt{2}$

19. Find the 4 fourth roots of

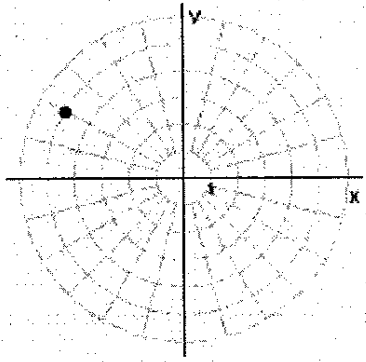
$$z = \cos \frac{10\pi}{9} + i \sin \frac{10\pi}{9}$$

- a. $\operatorname{cis} \frac{\pi}{4}, \operatorname{cis} \frac{3\pi}{4}, \operatorname{cis} \frac{5\pi}{4}, \operatorname{cis} \frac{7\pi}{4}$
- b. $\operatorname{cis} \frac{5\pi}{36}, \operatorname{cis} \frac{7\pi}{18}, \operatorname{cis} \frac{23\pi}{36}, \operatorname{cis} \frac{8\pi}{9}$
- c. $\operatorname{cis} \frac{13\pi}{36}, \operatorname{cis} \frac{31\pi}{36}, \operatorname{cis} \frac{49\pi}{36}, \operatorname{cis} \frac{67\pi}{36}$
- d. $\operatorname{cis} \frac{13\pi}{72}, \operatorname{cis} \frac{31\pi}{72}, \operatorname{cis} \frac{49\pi}{72}, \operatorname{cis} \frac{67\pi}{72}$
- e. $\operatorname{cis} \frac{5\pi}{18}, \operatorname{cis} \frac{7\pi}{9}, \operatorname{cis} \frac{23\pi}{18}, \operatorname{cis} \frac{16\pi}{9}$

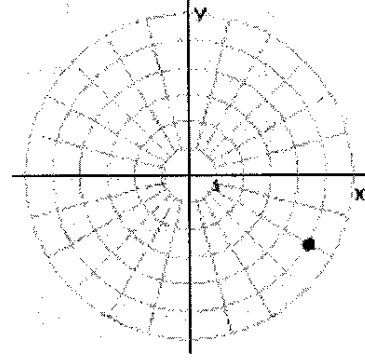
20. Graph the ordered pair on a polar coordinate system.

$$(5, 150^\circ)$$

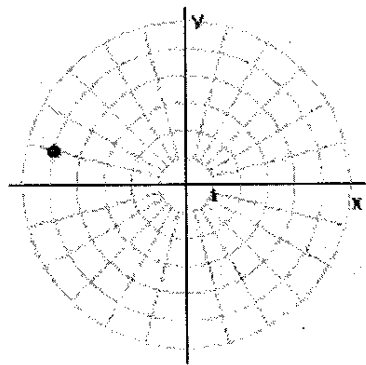
a.



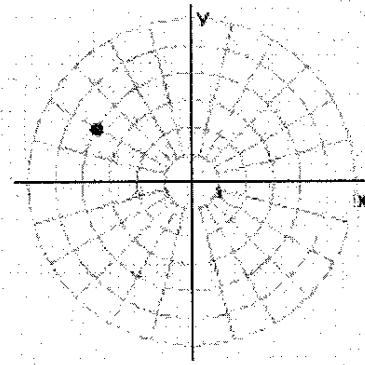
d.



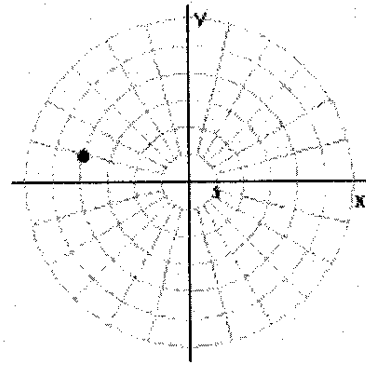
b.



e.



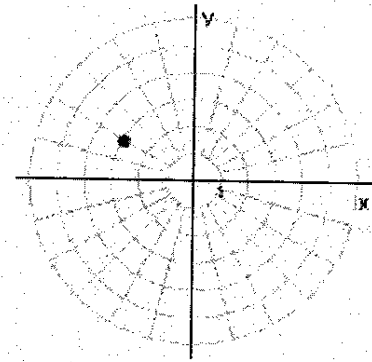
c.



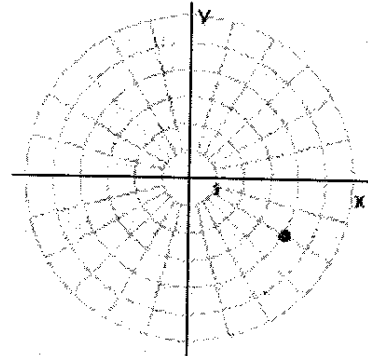
21. Graph the ordered pair on a polar coordinate system.

$$(4, -210^\circ)$$

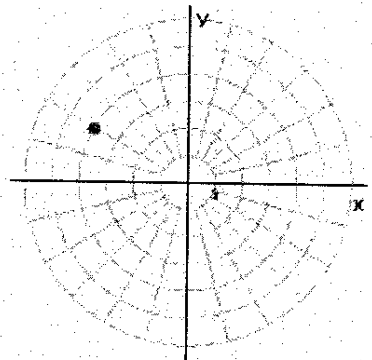
a.



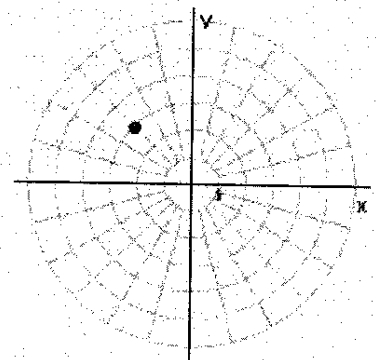
d.



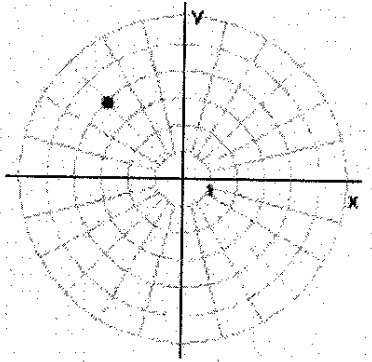
b.



e.



c.



- ___ 22. Convert to rectangular coordinates. Use exact values.

$$\left(9, \frac{\pi}{2}\right)$$

- a. (0, 9)
- b. (0, -8)
- c. (0, 7)
- d. (0, -9)
- e. (0, 8)

- ___ 23. Write the equation with rectangular coordinates.

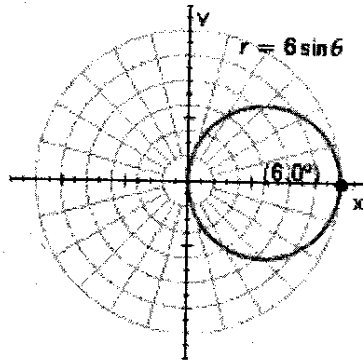
$$r = 7\cos \theta$$

- a. $x^2 - y^2 = 6x$
- b. $x^2 + y^2 = 7x$
- c. $x^2 - y^2 = 7x$
- d. $x^2 + y^2 = 6x$
- e. $x^2 + y = 7x$

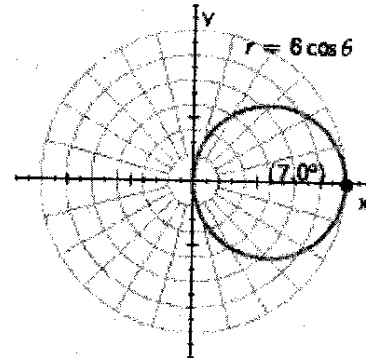
24. Convert the equation to polar coordinates and then sketch the graph.

$$x^2 + y^2 = 6x$$

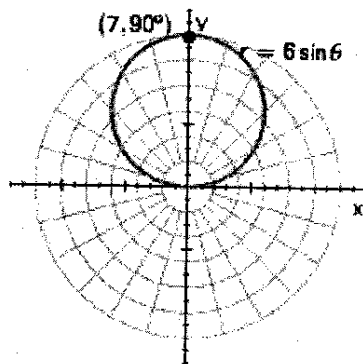
a.



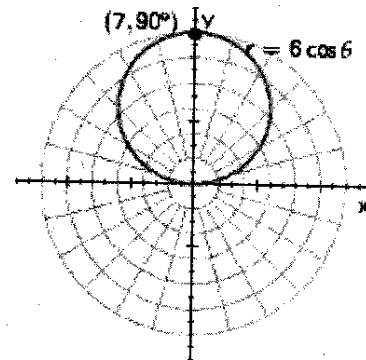
d.



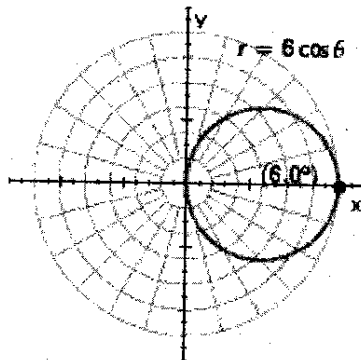
b.



e.



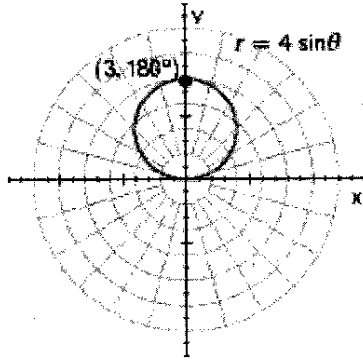
c.



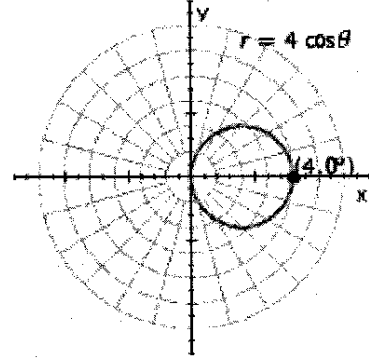
25. Convert the equation to polar coordinates and then sketch the graph.

$$x^2 + y^2 = 4y$$

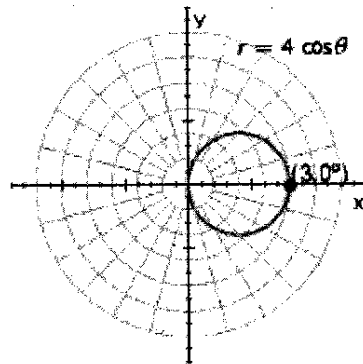
a.



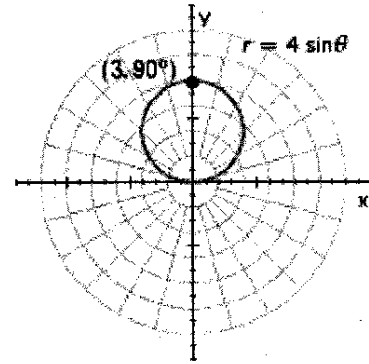
d.



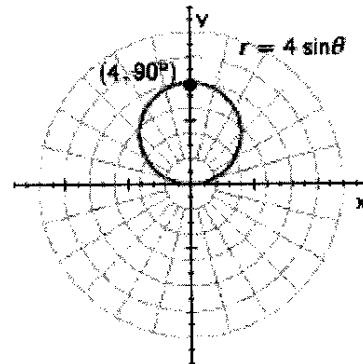
b.



e.



c.



Chapter 8
Answer Section

MULTIPLE CHOICE

- | | |
|------------|--------|
| 1. ANS: A | PTS: 1 |
| 2. ANS: D | PTS: 1 |
| 3. ANS: E | PTS: 1 |
| 4. ANS: B | PTS: 1 |
| 5. ANS: B | PTS: 1 |
| 6. ANS: D | PTS: 1 |
| 7. ANS: A | PTS: 1 |
| 8. ANS: E | PTS: 1 |
| 9. ANS: E | PTS: 1 |
| 10. ANS: C | PTS: 1 |
| 11. ANS: A | PTS: 1 |
| 12. ANS: E | PTS: 1 |
| 13. ANS: B | PTS: 1 |
| 14. ANS: C | PTS: 1 |
| 15. ANS: B | PTS: 1 |
| 16. ANS: E | PTS: 1 |
| 17. ANS: C | PTS: 1 |
| 18. ANS: D | PTS: 1 |
| 19. ANS: E | PTS: 1 |
| 20. ANS: A | PTS: 1 |
| 21. ANS: B | PTS: 1 |
| 22. ANS: A | PTS: 1 |
| 23. ANS: B | PTS: 1 |
| 24. ANS: C | PTS: 1 |
| 25. ANS: C | PTS: 1 |

Chapter 8

Multiple Choice

Identify the choice that best completes the statement or answers the question.

___ 1. Write the expression $\sqrt{-36} \cdot \sqrt{-16}$ in terms of i and then simplify.

- a. 24
- b. -28
- c. 28
- d. -24
- e. -18

___ 2. Combine the complex numbers.

$$(10 - 8i) - (2 - 3i)$$

- a. $8 - 5i$
- b. $7 - 5i$
- c. $7 + 6i$
- d. $8 - 6i$
- e. $7 - 6i$

___ 3. Find the product.

$$(7 - 5i)^2$$

- a. $24 - 70i$
- b. $26 - 72i$
- c. $-26 - 72i$
- d. $24 - 72i$
- e. $26 - 70i$

___ 4. Find the product.

$$(2 + 7i)(2 - 7i)$$

- a. 49
- b. $53 - 28i$
- c. 51
- d. $51 - 28i$
- e. 53